

1. A roller rink charges a certain fixed amount to rent their facilities, and a separate amount for each guest. A party for 52 people cost \$410, and another party for 84 people cost \$578. Find the fixed amount to rent the rink, and the amount charged for each guest. **Show your work and label your answer!**

$x = \text{fixed cost}$ $y = \text{cost per guest}$

Equation #1 $x + 52y = 410$

Equation #2: $x + 84y = 578$

$$\begin{array}{r} x + 52y = 410 \\ -x - 84y = -578 \\ \hline \end{array}$$

$$\begin{array}{r} -32y = -168 \\ \underline{-32} \quad \underline{-32} \\ y = \$5.25 \end{array}$$

$$x + 52(5.25) = 410$$

$$\begin{array}{r} x + 273 = 410 \\ -273 \quad -273 \end{array}$$

$$x = \$137$$

The fixed amount to rent the rink is \$137, and they charge \$5.25 for each guest.

2. Traveling downstream, a boat can cover 16 kilometers in 2 hours. Going upstream, it can make only $\frac{3}{4}$ of this distance in 2 hours. What is the rate of the boat in still water and what is the rate of the current? **Show your work and label your answer!**

$r \times t = d$

$$\frac{16 \cdot \frac{3}{4}}{2} = 12$$

$x = \text{speed of boat}$
 $y = \text{current speed}$

Equation #1 $(x + y)2 = 16 \text{ km}$

Equation #2: $(x - y)2 = 12 \text{ km}$

$$\begin{array}{r} \div 2 \Rightarrow x + y = 8 \rightarrow 7 + y = 8 \\ x - y = 6 \end{array}$$

$$y = 1 \text{ km/hr}$$

$$\begin{array}{r} 2x = 14 \\ \underline{2} \quad \underline{2} \end{array} \quad x = 7 \text{ km/hr}$$

The rate of the boat in still water is 7 km/hr, and the rate of the current is 1 km/hr.

3. Graph the solution set to the system of inequalities. **Shade what is true.**

$$2x + 3y \geq 6 \rightarrow \frac{3y}{3} \geq \frac{-2x + 6}{3}$$

$$2x - y < 7$$

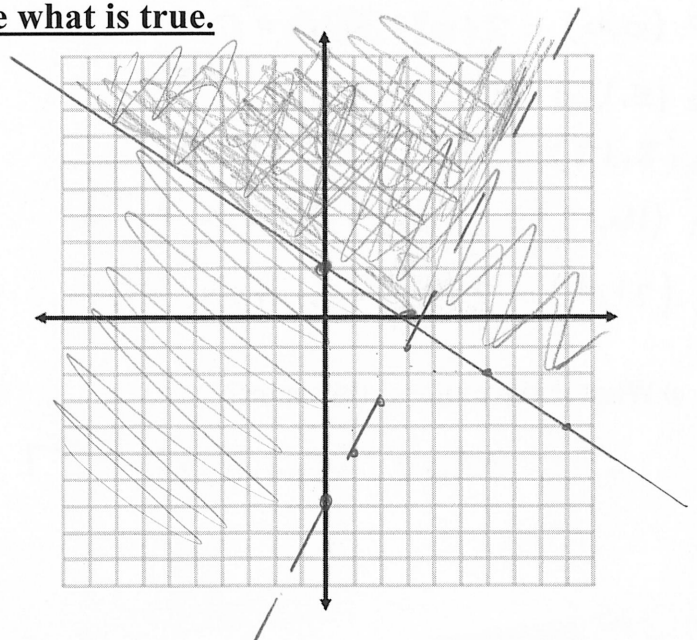
$$\frac{-2x}{-2} \quad \frac{-2x}{-2} \quad y \geq \frac{-2}{3}x + 2$$

$$-y < -2x + 7$$

\downarrow
 $\frac{-1}{-1} \quad \frac{-1}{-1} \quad \text{Shade Above / Solid line}$

$$y > 2x - 7$$

\downarrow
Shade Above
Dashed Line



4. You own a small greenhouse and plan to raise carnations and daisies. **Let x =carnations, and y =daisies.** Write an inequality for each of the following restrictions. **Graph each inequality, and shade what is false.**

a) The most you can plant is 46 plants total.

$$x + y \leq 46 \rightarrow y \leq -x + 46$$

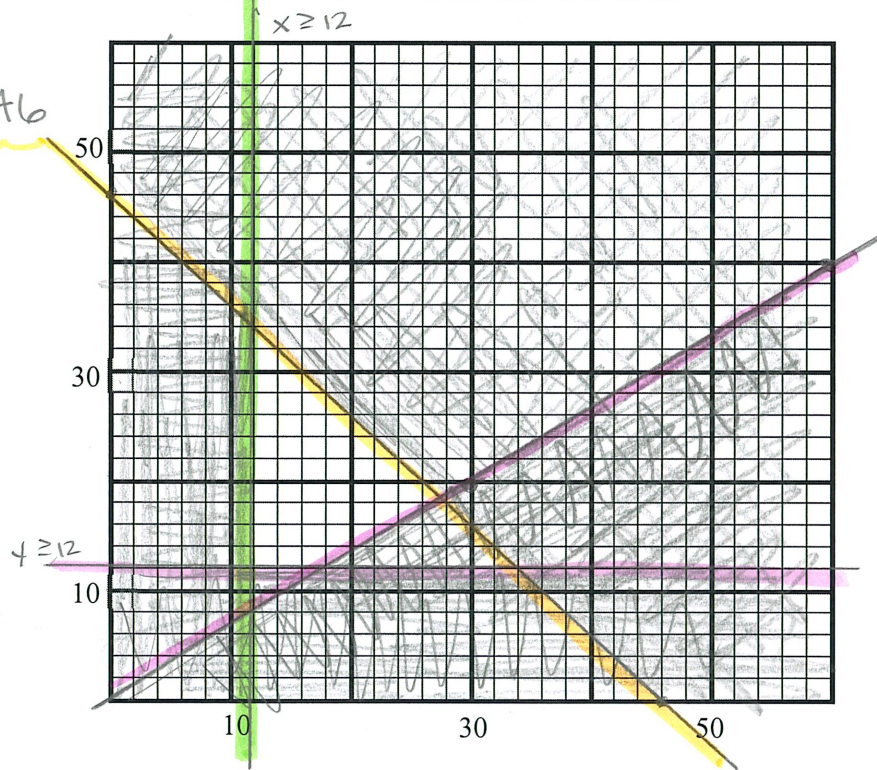
b) You must have at least 12 plants of each kind. (Hint: You need two inequalities for this part.)

$$x \geq 12$$

$$y \geq 12$$

c) The number of daisies must be greater than or equal to $\frac{2}{3}$ times the number of carnations.

$$y \geq \frac{2}{3}x$$



5. The following graph has been completed for a poultry farm. **The number of geese is on the x-axis, and the number of turkeys is on the y-axis.** The feasible region is shaded. A goose brings in a profit of \$2.00 and a turkey brings in a profit of \$3.00.

a) Write the equation representing total profit in terms of geese and turkeys.

$$\text{Profit} = 2x + 3y$$

b) Find the coordinates of the point for the maximum profit.

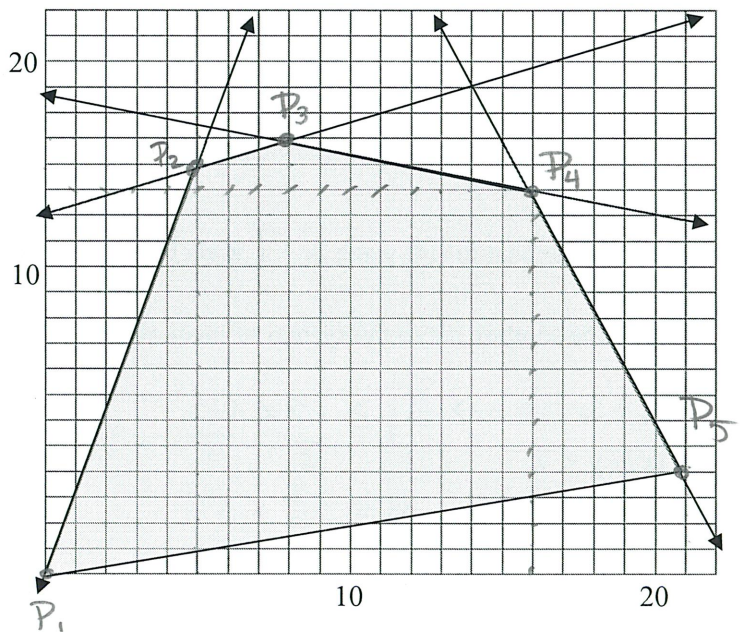
$$P_1(0,0) = 2(0) + 3(0) = 0$$

$$P_2(5,16) = 2(5) + 3(16) = \$58$$

$$P_3(8,17) = 2(8) + 3(17) = \$67$$

$$P_4(16,15) = 2(16) + 3(15) = \$77$$

$$P_5(21,4) = 2(21) + 3(4) = \$54$$



c) What is the profit at this point?

Max Profit = \$77 at 16 geese and 15 turkeys.